Statistically Defining Optimal Conditions of Coagulation Time of Skim Milk

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Summary: Milk consists a huge amount of largely water and different proteins. Kappa-kasein of these milk proteins can be coagulated by Mucor miehei rennet enzyme, an aspartic protease which cleaves 105 (phenylalanine)-106 (methionine) peptide bond. It is commonly used clotting milk proteins for cheese production in dairy industry. The aim of this study was to measure milk clotting times of skim milk by using Mucor Miehei rennet and determination of optimal conditions of milk clotting time by mathematical modelling. In this research, milk clotting times of skim milk were measured at different pHs (3.0, 4.0, 5.0, 6.0, 7.0, 8.0) and temperatures (20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75 °C). It was used statistical approach for defining best pH and temperature for milk clotting time of skim milk. Milk clotting activity was increased at acidic pHs and high temperatures.

Keywords: Milk clotting time, Mucor miehei Rennet, S curve, skim milk, optimization.

Introduction

Chymosin (calf rennet) – extracted from the fourth stomach (abomasum) of the young calves – has been used worldwide in cheese production for years and it has been preferred for its high quality. However, nowadays there has been a shortage of the chymosin in the world market, so proteolytic enzymes from different sources gained more importance [1].

Mucor miehei rennet is the most thermostable enzyme of Mucor miehei at acidic pH. It is an aspartic protease which cleaves 105 (phenylalanine)-106 (methionine) peptide bond in kappa-kasein (milk protein) [2, 3]. The aspartic proteinases (EC 3.4.23) display optimum activity at acidic pHs. Chymosin enzyme is aspartic proteinase that is traditionally used in the cheese making. Aspartic proteinases provide Endothia parasitica and Mucor miehei [4]. Casein micelles are stabilized by k-casein molecules in which casein hydrophobic parts and the hydrophilic surroundings. Tertiary structure of the protein are organized by the casein micelles [5, 6]. Coagulation of milk by rennet enzyme occurs in two steps. Firstly, casein micelles are degraded by using chymosin enzyme and afterwards degraded casein micelles automatically come together in the second step, according to the von Smoluchowsky model [7, 8].

Mathematical models (nonlinear least squares, etc.) are very useful for defining optimal conditions in different study subjects [9, 12]. In curve fitting data, the prevailing assumption regarding model description is that the construction is linear in the model coefficients. In many areas of fundamental sciences and engineering, disciplines having about empirical state proposes using of a less experimental, more theoretically based, nonlinear model.

The literature is quite rich in algorithms for the minimization of residual sum of squares in nonlinear model situations. In addition, there are many regression computer packages available that contain at least one nonlinear estimation method [11, 12].

In the literature, Ataci et al (2009) studied with Mucor miehei rennet at different pHs and temperature and they did only variance analysis [13]. Differently, optimum conditions of milk clotting times were investigated statistically with a mathematical equation (1) by using SPSS 18 program in our study and Fig. 2 was drawn according to this equation.

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The objective of this study to measure coagulation time of skim milk by using Mucor miehei rennet at different pHs and temperatures, and determination of optimum milk clotting time with mathematical model depending on experimental data.

Results and Discussion

Milk solution coagulated before adding enzyme because of the high acidity at pH: 3.0. Therefore, milk clotting activity was not determined at this pH. In Fig. 1 was shown that Mucor Miehei Rennet displays high milk clotting activity at low pH values. Milk solution was coagulated as soon as possible at acidic pHs. However, milk clotting activity is low at pH 7.0 and pH 8.0.

Mathematical Modeling

There are many examples of nonlinear models. We offer but a few here as illustrations:

$$y = \alpha e^{\beta x} + \epsilon$$  \hspace{1cm} (1)

The parameter(s) bring about a nonlinear model. The hard of model is the estimation of parameters. One of the most famous numerical technique is least square technique.

Nonlinear Least Squares

The improvement of the estimators which are more challenging from in linear model is possible via exponential regression model of Eq. (1). Given a set of data \((y_i, x_i)\) for \(i = 1,2,\ldots,n\) the estimators of \(\hat{\alpha}\) and \(\hat{\beta}\) are found by minimizing:

$$SS_{res} = \sum_{i=1}^{n} (y_i - \hat{\alpha} e^{\hat{\beta} x_i})^2$$  \hspace{1cm} (2)

Differentiation of (2) with respect to \(\hat{\alpha}\) and \(\hat{\beta}\) and set each derivative to zero. This yields:

$$\sum_{i=1}^{n} (y_i - \hat{\alpha} e^{\hat{\beta} x_i}) (-e^{\hat{\beta} x_i}) = 0$$

$$\sum_{i=1}^{n} (y_i - \hat{\alpha} e^{\hat{\beta} x_i}) (-\hat{\beta} e^{\hat{\beta} x_i} x_i) = 0$$  \hspace{1cm} (3)

Estimation of \(\hat{\alpha}\) and \(\hat{\beta}\) parameters need some numerical iteration methods in nonlinear equation (3).

Graphics was drawned according to mathematical equation (1) by using SPSS 18 program in Fig. 2. All the results (except pH 8) obeyed S type curve. Because of this reason, we use S type curve for temperature and pH estimation. It was decided that S curve compliance with experimental observed milk clotting time values (Fig. 2).

Experimental

Materials

Mucor miehei rennet was purchased from Sigma. Skim milk powder was supplied by Pinar Co. Ltd. (Izmir, Turkey). Specifications of skim milk powder can be shown in the Table-1. Calcium chloride, 97 % powder, was obtained from Riedel-de Haen (Cat.: 12095). Other reagents were used of analytical grade.

<table>
<thead>
<tr>
<th>Energy</th>
<th>363 kcal</th>
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<tbody>
<tr>
<td>Protein</td>
<td>36 g</td>
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<tr>
<td>Carbohydrate</td>
<td>52 g</td>
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<tr>
<td>Calcium</td>
<td>1256 mg</td>
</tr>
<tr>
<td>Fat</td>
<td>1.25 g</td>
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</tbody>
</table>

Preperation of Skim Milk Solution

Milk were prepared fresly from powder skim milk in a 2 L beaker. 50 g skim milk powder (10 %) was weighed and added to 500 mL buffer solution (acetate buffer pH: 5.0) than milk was mixed and than left for 30 min. to rest.
Fig. 1: Milk clotting activity (IU/mg) of *Mucor miehei* rennet at different pHs and temperatures.

Fig. 2: Milk clotting times of *Mucor Miehei* Rennet at different pHs and temperatures. (○ experimental observed, --- Cubic, - - - S, --- Exponential)
Determination of Milk Clotting Time

From fresh milk solution, 10 mL milk solution transferred into a 25 mL beaker in which water bath at different temperatures and pHs. Afterwards, *Mucor Miehei* rennet enzyme (0.04 mg mL⁻¹) was added to skim milk solution and coagulation time was determined according to visual method of Hostettler [14]. Aliquots (10 ml) of skim milk solution (at desired pH and temperature) were placed in separate beakers (each volume of them 25 mL) and tempered at desired temperature for 5 min. After 1 mL of enzyme solution were added to each beaker, the coagulation time was measured as the time required for the first occurrence of clots on the surface of the glass walls of beaker in the milk solution [15]. Milk clotting times of *Mucor miehei* rennet were measured at different pHs and different temperatures. Results of milk clotting time of skim milk at different circumstances can be shown in the Table-2. All milk clotting experiments were conducted with three replicates.

Table-2: Milk clotting times (sec.) of *Mucor miehei* rennet at different pHs and temperatures.

<table>
<thead>
<tr>
<th>Temperature (°C)</th>
<th>pH: 4</th>
<th>pH: 5</th>
<th>pH: 6</th>
<th>pH: 7</th>
<th>pH: 8</th>
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<tbody>
<tr>
<td>20</td>
<td>201</td>
<td>237</td>
<td>247</td>
<td>564</td>
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<tr>
<td>25</td>
<td>87</td>
<td>112</td>
<td>140</td>
<td>289</td>
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<td>69</td>
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<tr>
<td>75</td>
<td>15</td>
<td>5</td>
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</tr>
</tbody>
</table>

* Milk solution was clotting by spontaneously without the addition of enzyme solution.
** Milk clotting was not observed after waiting 10 minutes. Each data point represents the average value of three independent experiments.

Conclusion

Milk clotting can occur two method; by acidification and enzyme. pH and temperature of skim milk were effect on milk clotting time. Milk solution was shortly clotting at low pHs and high temperature. In addition, increasing temperature also reduce milk clotting time and enhance milk clotting activity. Statistical approach was used for defining best pH and temperature for milk clotting time. Experimental data of this research are shown that equation for coagulation of milk is obeyed S curve. According to this research finding, researchers can be estimate milk clotting time for the same experimental conditions.

References